

Tim Mauldin:

On the unification of physics

Two questions:

- what is unification?
- why do we want unification?

Introduction

- "most radical transformation"
in last 300 yrs
- "velvet revolution"
(no opposing camps, no exp. evidence)

- unification = "combination" of ≥ 2 forces

→ \ni math. consistency
(i.e. no contradictions)

\ni common dynamics

e.g. $\vec{F} = -\vec{\nabla}V$, $V \in \{V_a, V_{em}\}$

but: V_a, V_{em} independent

\ni "law-like connection"

e.g. Maxwell-Eqs.: duality $\vec{E} \leftrightarrow \vec{B}$

but: ontologically different

• perfect unification

examples:

• special relativity:

$$\vec{E} \leftrightarrow \vec{B} \Rightarrow F_{\mu\nu}$$

↑
reference frame

• general relativity:

inertia + gravity \Rightarrow curved space-time

↑

$$\vec{F} = m_I \ddot{\vec{x}}$$

↑

$$V_G = G_N \frac{m_G M}{r}$$

$$m_I \equiv m_G$$

Unification in modern particle physics

- Standard Model:

strong + weak + e.m. interaction

$$SU(3) \otimes \boxed{SU(2) \otimes U(1)}$$

electro-weak

common dyn.
(gauge-int'n)

G_Y^a
 $a \in \{1, \dots, 8\}$

independent

$$\Rightarrow SU(3) \otimes EW$$

$$\sim V_G \otimes V_{e.m.}$$

$$\begin{matrix} W^+ \\ W^0 \\ W^- \end{matrix}, B \xrightarrow{\sin^2 \theta_W} (Z^0, A_\mu)$$

unification "at least as strong" as Maxwell
(true?)

- mixing \Rightarrow unification ?

Moriyasu : yes

Georgi : no

instead: simple group, e.g.

$$\text{GUT: } \mathfrak{g}_{\text{GUT}} = \mathfrak{g}_3 \otimes \mathfrak{g}_2 \otimes \mathfrak{g}_1$$

- 3 levels : 1) product group w/o mixing
 2) - " - with - " -
 3) simple group : GUT

Simplicity vs. Complexity

- $SU(5)$ itself is — in some sense — **simple**:
similar to QCD ($= SU(3)$)
- needs to be **broken**!
↳ many new parameters
- need **Higgs fields** (ad-hoc?)

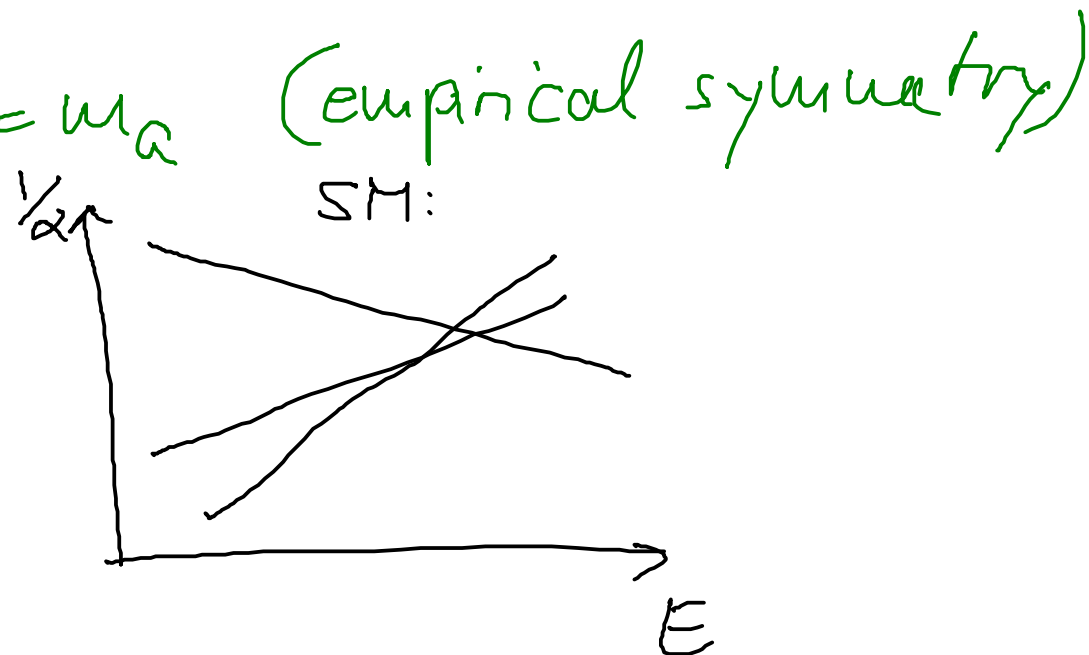
Why unification?

- exp. evidence?

e.g. gravity: $m_I = m_a$ (empirical symmetry)

in particle physics?

- $\sin^2 \Theta_w^{\text{GUT}} \approx \sin^2 \Theta_w^{\text{exp}}$



- aesthetic reasons?

Theory of Everything (TOE)

• SM + Gravity

problems: - "gravity is not a force"

- QFT in curved space-time?

- $M_{\text{cut}} \approx 10^{16} \text{ GeV} \ll M_{\text{Planck}} \approx 10^{19} \text{ GeV}$

Conclusions

- upper + lower bounds for unification
- motivation: emp. symmetries
in particle physics?
- $SU(2) \otimes U(1)$ "more" unified than $SU(3) \otimes EW$?
- GUT
- TOE

Thoughts

- several open / controversial issues
- tight relation to hierarchy - project
($m_{\text{Bare}}^{\text{Higgs}} \approx m_{\text{vacuum}}^{\text{Higgs}}$)
- physicist?